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Cavity diameter and height of cyclodextrins and cucurbit[*n*]urils from the molecular electrostatic potential topography

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Abstract Understanding the interactions of cyclodextrins (CD) and cucurbit[n]uril (CB[n]) hosts with a variety of guest molecules following their encapsulation within the cavity of these macrocycles have become increasingly important in the recent years. The electronic charge distribution and the cavity dimension are some of the key factors those govern their interactions with cations or neutral guests. In the present work the molecular electrostatic potential (MESP) topography has been utilized to obtain the 'effective' cavity diameter and height of CB[n] (n = 6-8) homologues and 8 conformers each of α -, β - and γ -CD. It has been shown that the shape of CD cavity be it cone- or barrel-like stems from the hydrogen bonding patterns within primary hydroxyl groups. The width of CB[7] is comparable to the β -CD conformer that possesses either O₆H–O₅' or intraglucose O₆H–O₅ interactions. The cavity diameters of α - and γ -CD are predicted to be respectively, 1.0 and 1.5 Å larger than CB[6] and CB[8] hosts. MESP topography reveals that the cavities of CB[n] are less hydrophilic with largely hydrophilic portals as compared to CD hosts. Cremer-Pople puckering parameters were derived for all the CD conformers and CB[n]. It has been demonstrated that the clockwise and anticlockwise hydrogen bonding patterns in the lower as well as upper rims of different CD conformers are less distorted and exhibit a little deviation from the $^{\circ}C_3$ chair conformation of α -D-glucopyranose constituting monomeric unit of CD.

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R. V. Pinjari · J. K. Khedkar · S. P. Gejji (⊠) Department of Chemistry, University of Pune, Ganeshkhind, Pune 411007, India e-mail: spgejji@chem.unipune.ernet.in **Keywords** Cyclodextrins · Cucurbit[*n*]urils · Density functional theory · Molecular electrostatic potential · Cavity dimension

Introduction

Cyclodextrins (CD) are cyclic oligomers of glucose obtained from the enzymatic degradation of starch by cyclodextrin glucatranferase enzyme in intramolecular transglycosylation reaction [1]. The commercially available forms of CD are composed of $\alpha(1 \rightarrow 4)$ linkage of 6–8 glucopyranoside units. CD are capable of encapsulating compounds such as straight or branched chain aliphatics, aldehydes, ketones, alcohols, organic acids, fatty acids, aromatic and polar compounds and form inclusion complexes in solid state [2, 3]. The guest molecules with varying size can be accommodated in the CD cavity in solution as well [4, 5]. Inclusion of guest molecule within the cavity of the host protects it from oxidation, reduction or hydrolysis, decreases sublimation as well as volatility [6] and thus alters its physical or chemical properties [7]. Along with this the enhanced stability and water solubility of a drug molecule confined within the CD cavity leads to a controlled releasing ability [8, 9], improved bioavailability [10] and reduces its toxicity [11, 12].

It should be remarked here that the cavity size and the binding ability of CD towards different guests are often compared [12–15] with CB[n], cyclic oligomers of gly-couril units linked by a pair of methylene group [16], which represent a different family of hosts [17]. Like CDs, the CB[n] macrocycles offer varying cavity size and regioselectivity toward binding of variety of guests with the enhanced solubility in different solvents. Hydrophilic portals of CB[n] bind to metal ions [18, 19], inorganic salts

[20], whereas its hydrophobic cavity accommodates organic dyes [21], protonated alkyl/aryl [22] or platinum amine [23]. Host–guest interactions in such systems led to a wide range of applications in the recent years that include drug delivery [24, 25], separation technology [26], catalysis [27], rotaxanes [28] and nanotechnology [29].

To understand the host–guest interactions of α -, β - and γ -CD and their inclusion complexes calculations at different levels of theory, that include molecular mechanics [30–34], semi-empirical methods [35-39], Hatree-Fock, density functional methods [40-43] and simulations based on molecular dynamics [44] have been carried out. Topography of scalar fields such as molecular electron density (MED) or molecular electrostatic potential (MESP) have successfully been utilized to analyze hydrogen bonded interactions from the primary as well as secondary hydroxyl groups of α -, β - and γ -CD [42, 43]. Theoretical investigations on CB[n] homologues along with their inclusion complexes are also reported [45-49]. These results have shown that CB[6] and CB[7] hosts are largely stabilized over its acyclic polymer devoid of ring strain and large electrostatic repulsion due to ureido oxygens. It has been well known that matching of size and shape complimentarity of host and guest [50, 51] leads to substantial binding affinity toward the guest. Recent density functional calculations [45] have shown that the interaction of ferrocene with the CB[n] hosts tends to form inclusion complexes only with the CB[7] and CB[8] homologues while interacts laterally in case of CB[6]. Several molecular recognition theories have been put forth which highlights on the complementarity of guests in terms of size and shape for hosts [52]. This further necessitates quantifying the dimensions (diameter and height or depth) of the host cavity. As a pursuance to this we present a systematic MESP based approach to estimate "effective cavity dimensions" of CB[n] as well as those of CD hosts exhibiting different hydrogen bonding patterns in their conformations. The shape of host cavity can be further also be gauged from the charge distribution in terms of the MESP topography. To this end 24 different conformers of α -, β - and γ -CD, including all the 3 CD conformers reported earlier in Ref. [42], have been considered. This method enables one to compare directly the cavity dimension of different host families and therefore, should serve as an initial step toward the molecular level understanding of the host-guest interactions.

Computational method

CB[*n*] (n = 6-8) homologues and 8 conformers each of α -, β - and γ -CD were optimized employing the density functional theory incorporating Becke's three-parameter

exchange with Lee, Yang, and Parr's (B3LYP) correlation functional [53, 54]. The internally stored 6-31G(d) basis set was used. Optimizations (without any symmetry constraint) were performed using the GAUSSIAN 03 program [55]. The molecular electrostatic potential (MESP), V(r) in these hosts have been calculated. The V(r) essentially comprised of two terms with one representing the repulsion between the positive probe and nuclei and the second term is its attraction to the electrons; the latter essentially represents the columbic interactions between the charge and the electrons. Substantial effective negative values in V(r)arising from the net balance of aforementioned electronic and the bare nuclear contributions reveal regions conducive to electrophilic interactions. The MESP exhibits rich topographical features, which has subsequently been mapped by examining eigenvalues of the Hessian matrix at the point where gradient V(r) vanishes and thus the critical points (CPs) were located using the code written in our laboratory [56]. The CPs are characterized in terms of an ordered pair (R, σ), where R and σ denote the rank and signature (i.e. the sum of algebraic signs of the eigen values) of the Hessian matrix, respectively. These CPs can further be grouped into three sets: (3,+3) as local minima and (3,+1) or (3,-1) which correspond to saddle points. Interestingly lone pairs on electronegative atoms in molecules can be inferred from (3,+3) CPs in the MESP topography. Furthermore the (3,+3) CPs (local minima) herein represent the potential binding sites of the host toward binding of an electrophile or the neutral guest [57, 58]. Thus the MESP topography has proven useful for modeling an electrophilic attack on a molecule. UNIVIS-2000 was utilized for visualization of the MESP along with its isosurface [59].

Results and discussion

Atomic numbering scheme and optimized geometry of a glucose residue cut out of CD is shown in Fig. 1a. Likewise Fig. 1b displays the glycouril monomer in CB[n]. Conformers possessing primary as well as secondary hydroxyl groups oriented in clockwise as well as anticlockwise fashion and combinations therein of α -, β - and γ -CD hosts were considered. CB[n] homologues yield only one conformer. Hydrogen bonding patterns at the primary hydroxyl groups allow CD conformers to be classified in three different classes with those comprising of (i) O_6H - O_6' interactions referred as "A", (ii) O_6H-O_5' interactions which are denoted by "B" and (iii) intra-glucose O₆H–O₅ interactions (involving ether oxygens) called as "C". The single prime here refers to atom from the adjacent glucose unit. These conformers of α -CD, as a prototype example, are displayed in Fig. 2 along with the CB[n] (n = 5-8)



Fig. 1 Atomic numbering scheme in **a** the glucose unit cut from CD and **b** glycouril unit in CB[n]

homologues. Different patterns of these hydrogen bonded interactions from primary and secondary hydroxyl functionalities yield four conformers of "A" denoted by A1, A2, A3, and A4. Here, 1 refers to the pattern where the hydroxyl protons oriented anticlockwise in top rim and clockwise in bottom rim; the conformer designated as 2 has exactly reverse orientations in both these rims. Furthermore, in the conformer labeled as A3, 3 denotes the hydroxyl protons arranged clockwise in both top and bottom rims and finally the conformer possessing the hydrogen bonding pattern opposite to that of conformer 3 are denoted by 4; that is hydroxyl groups in both these rims orient in anticlockwise manner. With these notations only B2, B3 conformers were derived in class "B". Likewise C1, and C4 conformers in class "C" can be characterized. Thus O_2H-O_3' interactions were noticed only in A2, A4, B2 and C4 conformers whereas rest of the conformers facilitate O_3H-O_2' interactions from the secondary hydroxyl groups of the bottom rim. It may further be stated here A1, B3, and C1 conformers possess the O_3H-O_2' hydrogen bonded interactions and turn out to be of lowest energy in the respective class.

The Cremer–Pople puckering parameters [60] viz. phase angle (Φ), magnitude of puckering (θ), and puckering amplitude (Q) which engender various possible conformations on the surface of sphere were obtained by using the Hyperchem macro and are given in Table 1. The Θ values in the A1–A4 conformers increase from α -, to γ -CD are all near zero or show a small deviation from it. This suggests the chair form of glucose. The distortion magnitude, Θ , for A1 or A3 is larger than those possessing anticlockwise orientation in the lower rim of CD hosts. Thus it should be remarked here that the A2 conformer in α -CD and similarly B2 and C1 of β -CD match well (the maximal deviation



Fig. 2 B3LYP optimized structures of "A", "B" and "C" conformers of α -CD and CB[n] (n = 5-8) homologues

Table 1 Cremer–Pople puckering parameters Φ , θ (in deg) and Q (in Å) in "A", "B", and "C" conformers of α -, β -, and γ -CD and CB[n] (n = 5–8) homologues

n:	6			7			8		
	Φ	θ	Q	Φ	θ	Q	Φ	θ	Q
CD									
A1	354.5	4.7	0.57	312.0	6.5	0.58	297.1	9.4	0.59
A2	332.6	2.9	0.57	288.6	5.8	0.58	279.3	8.8	0.59
A3	349.9	4.4	0.57	307.1	6.5	0.58	293.5	9.3	0.59
A4	340.3	3.1	0.57	294.5	5.8	0.58	282.6	8.7	0.59
B2	79.1	5.3	0.57	126.2	2.5	0.57	186.1	3.6	0.57
B3	57.8	6.1	0.56	60.3	1.9	0.56	228.4	1.4	0.56
C1	39.8	6.1	0.57	154.3	2.9	0.57	297.7	3.1	0.57
C4	63.5	4.7	0.57	87.5	0.5	0.57	234.3	2.5	0.58
CB[n]									
	144.0		0.04	143.0		0.05	147.4		0.06

being 0.5°) with the ideal value of the chair conformation of α -D-glucopyranose (2.7°) reported in the literature [61]. Furthermore as may be noticed Q, turns out to be the same for all the CD conformers and agree well with that obtained for the pyranoid ring (0.58 Å). Thus ring conformation (°C₃) for glucose, monomer of CD, has been predicted for these conformers. As opposed to this the phase angle (Φ) changes significantly with the relative orientations of primary hydroxyl groups as in the "A", "B" and "C" conformers. Relatively large values can be noticed for "A" conformers. Accordingly for the α -CD conformers these value turn out to be from 332.6° to 354.5° as opposed to

57.8° and 79.1° for the B2 and B3 conformers, respectively. For C1 and C4 conformers the corresponding values are predicted to be 39.8°, and 63.5°. It may also be noticed that the phase angle, Φ , decreases steadily in the "A" conformers with an increasing size of the macrocycle (α - to γ -CD) and thus in the A1 conformers of α -CD to γ -CD these values decrease from 354.5° to 297.1°. Further the A2 and A4 conformers possessing anticlockwise orientation of the secondary hydroxyl groups exhibit lower Φ values than those in the conformers A1 or A3 wherein the clockwise (O_3H-O_2') interglucose hydrogen bonding pattern can be noticed. It was pointed out earlier [42] that the strength of O₆H–O₆' interactions from the primary hydroxyls decreases steadily on going from α -CD to γ -CD. A similar trend was shown in the calculated Φ values of these conformers. The corresponding Φ values are quite different in the B2 and B3 conformers, those possess the anticlockwise and clockwise hydrogen bonding patterns in its bottom rim, respectively. Thus it may be inferred that the phase angle, (Φ) has largely been influenced by the hydrogen bonded interactions. The Φ values for the C1 and C4 displayed in Table 1 also support these conclusions. Cremer–Pople parameters of CB[n](n = 5-8) macrocycles are presented in Table 1. Here the puckering amplitude, (Q), turns out to be 0.05 ± 1 along CB[5] to CB[8] series which stems from the planar fivemembered rings of CB[n]. These inferences are in consonant with those reported for acylated glycourils in the literature [62].

It was pointed out in the preceding section that the MESP brings about the effective localization of electron-rich



Fig. 3 MESP mapped (from -131.28 to 266 kJ mol⁻¹) on CD and CB[n] conformers

regions and further vield insights for interaction of the host with electrophilic functionalities of the guest. An electrostatic potential in the CD compared with CB[n] (cf. Fig. 3) shows large electron-rich regions near glycosidic oxygens in CD, whereas its cavity turns out to be less electron-rich. An MESP isosurface ($V = -105.0 \text{ kJ mol}^{-1}$) in different α -, β - and γ -CD conformers and that in the CB[n] (n = 6-8) hosts are depicted in Fig. 1S. The electron-rich regions within the top rim of "A" conformers project outward whereas within the "B" and "C" conformers those direct toward the cavity concomitantly encompassing the openings of the cavity partially at the primary hydroxyl functionalities. As shown in Fig. 1S the lowest energy conformer in each of the aforementioned "A", "B" and "C" class emerge with small electron-rich regions near O_2 which predict that the O₃H–O₂' hydrogen bonded interactions are relatively strong and follow the rank order "C" > "B" > "A". As may further be inferred within the CB[n] homologues MESP isosurface extends within the cavity. This partly explains their large affinity toward cationic guests. The (3,+3) MESP minima in the α -, β - and γ -CD conformers and CB[n] homologues were identified. A lateral view of CPs in the lowest energy A1, B3, and C1 conformers of α -, β - as well as γ -CD and in the CB[n] macrocycles are displayed in Fig. 2S. The minima were assigned notations namely 'v' (shown in aqua) near ring oxygen O₅, 'w' (green) and 'w*'(olive green) those near primary hydroxyl oxygen O6 within and outside the cavity, 'x' (blue) near the glycosidic oxygen O₄ and finally 'y' (black) and 'z' (pink) that corresponding to O_2 and O_3 atoms from the secondary hydroxyl group, respectively. MESP value at these minima in α -, β - and γ -CD conformers are given in Table 2. The A1, B3, and C1 conformers engender deepest minima ('w') for the primary hydroxyl oxygen in the respective class. Accordingly the B3 conformer of α -CD yields a minimum with V =-240.4 kJ mol⁻¹ compared to a marginally (5.9 kJ mol⁻¹) shallow minimum for B2. On the other hand for α -CD the minima ('w') near primary hydroxyl oxygens in conformer "A" turns out to be shallow relative to those in β - and γ -CD. The "B" and "C" conformers render O_6 to be the electronrich. Furthermore, when O₃ is hydrogen bond acceptor (conformer 2 and 4 having O_2H-O_3' interactions) it renders electron rich nature in the α -CD. For example, in C4 conformer of α -CD the 'z' minimum near O₃ turns out to be $-124.2 \text{ kJ mol}^{-1}$ whereas shallow minima with V = -122.9 and -120.2 kJ mol⁻¹ were located in the C4 conformers of β - and γ -CD, respectively. Thus MESP topography suggests relatively strong O₂H–O₃' hydrogen bonded interactions in γ -CD. Similarly the deeper minima near O_2 are located in α -CD. These conclusions are in line with those drawn earlier from the calculated NMR chemical shifts and from the MED topography [43]. A large

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Table 2 MESP minima (in kJ mol⁻¹) in α -, β - and γ -CD conformers

	v	W*	W	х	У	Z
α-CD						
A1	-124.6	-177.5	-101.8	-98.1	-147.7	-175.6
A2	-114.2	-182.6	-56.7^{a}	-76.4^{a}	-184.1^{a}	-146.0^{4}
A3	-123.2	-190.5	-64.3	-93.9	-146.1	-171.8
A4	-116.2	-168.9	-93.9	-80.1	-188.3	-147.0
B2	-96.1		-234.5	-78.3	-174.1	-118.0
B3	-102.0		-240.4	-90.6	-127.1	-161.8
C1	-96.0		-232. 9	-89.1	-130.5	-166.6
C4	-90.9		-227.4	-76.9	-180.5	-124.2
β -CD						
A1	-124.7	-166.2	-125.5	-106.2	-147.2	-177.7
A2	-114.2	-157.9	-83.7	-83.5	-186.8	-144.1
A3	-123.3	-184.0	-94.4	-102.0	-144.5	-173.1
A4	-116.3	-157.4	-116.8	-88.9	-190.9	-147.1
B2	-94.1		-234.4^{a}	$-85.9^{\rm a}$	-174.7^{a}	-115.1
B3	-100.0		-240.3	-97.1	-127.3	-160.5
C1	-95.1		-231.4	-94.6	-130.9	-165.7
C4	-89.0		-225.6	-81.2	-180.1	-122.9
γ-CD						
A1	-124.4	-156.6	-140.6	-112.1	-145.9	-178.9
A2	-114.2	-168.2	-105.3	-88.9	-189.0	-145.0
A3	-123.2	-177.5	-113.8	-108.0	-143.5	-175.2
A4	-115.5	-147.5	-131.2	-94.2	-192.1	-147.1
B2	-93.4		-234.7^{a}	-91.1^{a}	-174.1^{a}	-112.4
В3	-98.4		-239.8	-101.4	-126.9	-158.9
C1	-95.0		-230.2	-98.5	-130.1	-164.9
C4	-88.6		-223.6	-85.0	-179.8	-120.2

^a Reference [42]

downshifted signal of hydroxyl (O_3H) proton relative to those bonded to O_2 was also observed in the measured NMR spectra [63]. The experimental observations are accordingly in line with these conclusions. Interestingly the semiempirical AM1 quantum chemical calculations pointed out that the secondary hydroxyl functions (O_2H , O_3H) of saccharides are more acidic than those from the primary hydroxyl functions [64]. It has also been noticed that the 'w' and 'x' CPs in CD cavity are sensitive to the cavity size, and become deeper in γ -CD.

MESP minima (in kJ mol⁻¹) both at the portals ('w') and within the cavity ('x') of CB[*n*] hosts are reported in Table 3. The minima ('w') near portal oxygens $(V = -277.5 \text{ kJ mol}^{-1})$ in the CB[6] were noticed to be deeper than those within the cavity ($V = -68.5 \text{ kJ mol}^{-1}$). As opposed to this, the CB[8] exhibits a deeper minimum (-85.1 kJ mol⁻¹) within the cavity and renders it to be largely electron-rich. It may, therefore, be inferred that unlike in CB[8], the cavity of its lower homologue CB[6] is less hydrophilic with its portals exhibiting large

Table 3	MESP	minima	in	CB[n]	(<i>n</i>	=	6-8)	hosts
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	ESP (in kJ mol ⁻¹)		
	w ^a	Х	
CB[5]	-299.31	-49.88	
CB[6]	-277.54	-68.52	
CB[7]	-262.01	-79.23	
CB[8]	-251.84	-85.14	

^a Reference [45]

hydrophilicity. The MESP minima near portal oxygens ('w') in CB[n] homologues are deeper than those identified near primary hydroxyl oxygens (O₆) of CD. The shallow minima were located within the cavity of CB[n] hosts. It may therefore, be concluded that CB[n] cavity possess less hydrophilic character than CD hosts, whereas its portals are predicted to be largely hydrophilic compared to those of CD.

In the following we outline how the MESP minima yield a measure of the effective cavity dimensions of CB[n] or CD. Here we gauge the diameter and the height of the cavity in a variety of α -, β - and γ -CD conformers (aforementioned "A", "B" and "C" classes) and further analyze how the cavity shape be it cone or barrel, can be governed by hydrogen bonded interactions from the upper and lower rims. For CD hosts, the 'w' CPs near primary hydroxyl functionalities and 'x' CPs near glycosidic oxygens (O₄) impart the characteristic shape to its cavity. Top view of these CPs ('w' and 'x') in the lowest energy A1, B3, and C1 conformers of β -CD and those within the CB[7] host, as prototype examples, are displayed in Fig. 4. A side view showing the separation of planes containing 'w' and 'x' CPs in figure yields the 'effective' cavity height within the host. A cone shaped cavity of β -CD is clearly discernable with the 'w' CPs being relatively nearer compared to the separation of 'x' CPs in its "A" type conformers. It is further evident that the separation of two planes containing 'w' and other with 'x' CPs for "B" and "C" type conformers is nearly the same and concomitantly led to a barrel shape cavity. In other words the barrel shaped cavity can be noticed not only for β - and γ -CD but also for the α -CD in the "B" and "C" conformers. A top view containing the array of 'w' and 'x' CP in α - and γ -CD and those in CB[6] and CB[8] are compared in Fig. 3S of the supporting information. As is evident the cavity shape whether cone or barrel is not dependent on varying number of glucose units in CD macrocycles but is primarily governed by hydrogen bonding patterns at the primary hydroxyl groups. As shown in Fig. 4 the CB[n] homologues exhibit barrel-shaped cavity and unlike in CD two planes associated with different sets of 'x' CPs may be noticed for the CB[n] hosts. Hence the CD and CB[n] macrocycles herein show distinct electron distribution characteristics within the cavity.

The cavity diameter and the cavity height can be estimated by exploring the MESP topography. The cavity diameters of CB[n] portals and the CD rims were calculated from the separation between the radially opposite critical points in the MESP topography. An average separation of the radially opposite CPs yields the cavity diameter. The cavity height can be derived as follows: the x, y, z coordinates of all the (3,+3) CPs have been transformed to a new coordinate system, wherein the Z-coordinates of 'w' CPs in the CD hosts (or one of the portals in case of CB[n] homologues) were set to zero. Consequently the cavity has been set parallel to the Z-axis and thus the planes formed by different set of CPs become perpendicular to the axis. The z-coordinate of the CPs in a given plane turn out to be nearly identical in the coordinate framework defined here. Accordingly the cavity height in the α -, β -, and γ -CD can be calculated from the separation between two planes, viz., one formed by the CPs in the top rim ('w') and the other resulting from those within the cavity ('x').



Fig. 4 Top view of array of MESP CP ('w' and 'x') in β -CD and CB[7]. Planes comprising of CPs 'w' and 'x' in β -CD and CB[7] are shown. See text for details

The cavity diameter and the cavity height of α -. β - and γ -CD conformers thus obtained are given in Table 4. For the "A" conformers of α -CD the upper and lower rim diameters (d_w and d_x) turn out to be 4.38 and 7.01 Å, respectively. The upper rim diameter has been noticed to be less sensitive to hydrogen bonding patterns in the secondary hydroxyl groups; the diameter of lower rim on the other hand, varies from 6.39 to 7.01 Å in the A1-A4 conformers. The lower rim diameters in β - and γ -CD conformers are nearly 3.0 and 3.5 Å larger than those calculated for the upper rim. In "B" and "C" conformers both d_w and d_x estimated to be nearly the same. The cavityheight, separation of planes formed by 'x' and 'w' CPs, reported in Table 4 turn out to be largest for the "C" conformers (8.6-8.8 Å) than those for "B" or "A" conformers of CD hosts. Thus the cavity height does not vary significantly within the given class of CD conformers.

The diameter and height of the CB[n] homologues can also be derived using the methodology similar to that for CD hosts outlined earlier. Here the effective cavity height (h_{ww}) for CB[n] can be obtained from the separation of planes constituting the 'w' CPs one each at both the portals of host. The separation of two planes, viz., one containing the 'w' CPs at the portal and the other defined by 'x' CPs (midway between the two portals shown in Fig. 4) provides

Table 4 Cavity diameter of top (d_w) and bottom (d_x) rim and cavity height (h_{wx}) (in Å) in α -, β - and γ -CD

	α-CD			β -CD			γ-CD		
	$\overline{d_w}$	d_x	\mathbf{h}_{wx}	$d_{\rm w}$	d_x	\boldsymbol{h}_{wx}	$\mathbf{d}_{\mathbf{w}}$	d_x	\boldsymbol{h}_{wx}
A1	4.38	6.80	6.04	5.40	8.34	5.58	6.75	10.34	5.12
A2	4.34 ^a	6.39 ^a	5.86 ^a	5.28	8.10	5.48	6.55	10.03	5.08
A3	4.35	7.01	6.48	5.28	8.53	6.05	6.57	10.52	4.96
A4	4.38	6.49	5.47	5.38	7.98	5.03	6.74	9.90	4.57
B2	6.41	6.16	6.64	7.56 ^a	7.63 ^a	6.33 ^a	9.14 ^a	9.50 ^a	6.13 ^a
B3	6.36	6.13	6.83	7.49	7.60	6.50	9.08	9.47	6.23
C1	6.87	6.21	8.59	7.92	7.70	8.81	9.39	9.57	8.82
C4	6.82	6.17	8.33	7.87	7.62	8.47	9.43	9.46	8.48

See the text for details

^a Reference [42]

Table 5 Cavity diameter and cavity height (in Å) of CB[n] (n = 5-8) hosts

	d^{a}_{w}	d_x	h _{xx}	$\mathbf{h}_{\mathbf{w}\mathbf{x}}$	$h^{a}_{ww} \\$
CB[5]	3.92	4.30	1.99	5.94	13.88
CB[6]	5.51	5.88	2.06	6.06	14.18
CB[7]	7.06	7.13	2.07	6.18	14.42
CB[8]	8.54	8.57	2.23	6.19	14.55

^a Reference [45]

the estimate of h_{wx} . The diameter (d_w , and d_x), and heights (h_{xx} , h_{wx} and h_{ww}) thus obtained are presented in Table 5. As may readily be noticed along CB[*n*] series, h_{ww} turns out to be ~14.0 Å and remains nearly unchanged. The distinct electronic distribution within the CB[*n*] cavity can readily be noticed from the different values of h_{wx} and h_{ww} . As displayed, the cavity diameter of the upper rim of CB[5] turns out to be nearly less than one-half as compared to that for CB[8] homologue. Thus it may be inferred that penetration of the large guest within the CB[5] cavity will be relatively difficult and accordingly the CB[5] host does not conduce the inclusion complex. The earlier observation that ferrocene can not be encapsulated within the CB[5] cavity [45] can also be explained on similar lines.

A comparison of cavity dimensions in CB[*n*] and CD hosts reveals that both upper and lower rim diameters of "B" and "C" conformers in γ -CD (exhibiting barrel-like cavity) are 0.5–1.0 Å larger than those of CB[8]. Similar inferences may be drawn in case of α -CD and CB[6] hosts. On the other hand 'effective cavity diameter' of β -CD and CB[7] are comparable. It may be worth noting that cavityheight of CB[*n*] homologues are 5–6 Å larger compared to the "C" conformer of CD hosts exhibiting larger height.

Conclusions

This work presents a systematic investigations on the cavity size and molecular electrostatic potential topography in CB[n] (n = 5-8) and different ("A", "B" and "C") α -, β - and γ -CD conformers. It has been demonstrated how the 'effective' cavity height and diameter in different CD conformers can be gauged from the MESP topography. In case of α -, β - and γ -CD, the cavity shape is dependent on hydrogen bonding patterns from primary hydroxyl groups and not on the number of repeating sugar units in the macrocycle. Thus, "A" type conformers of α -, β - and γ -CD yield "cone-like cavity" while "B" and "C" conformers possesses a "barrel shaped cavity". The largest cavity height (8.6-8.8 Å) was noticed within the "C" conformers (possessing O_6H-O_5 interactions) of α -, β - and γ -CD. Cavity width (diameter) in the conformers facilitating either O_6H-O_5' or O_6H-O_5 interactions (as in the "B" and "C" conformers) turns out to be nearly the same. Furthermore the cavity diameter estimated from the MESP topography reveal that the width of CB[7] is comparable to "B" or "C" conformers of β -CD whereas that of α - and γ -CD are 1.0–1.5 Å larger compared to the CB[6] and CB[8], respectively. The distinct electronic charge distribution within the CB[n] (n = 6-8) cavity may also be noticed from the separation of planes constituting the MESP minima. On the other hand, the portals of CB[n]cavity turn out to be hydrophilic. This partly explains

large affinity of CB[n] hosts toward the cations or metal ions. The cavity-height of CB[n] homologues are relatively large (5–6 Å) compared to "C" type conformers of CD hosts. Furthermore the calculated phase angle Φ in the Cremer–Pople parameters depends on the type of hydrogen bonded interaction as well as hydrogen bond strength. In brief, the host–guest interactions at the molecular level can be analyzed by exploring the MESP topography.

Supporting information

The lateral view of (3,+3) CPs, top view of array of CP 'w' and 'x' in the electrostatic potential topography, MESP isosurface ($V = -105.0 \text{ kJ mol}^{-1}$) for the conformers of α -, β - and γ -CD as well as CB[n] (n = 6-8) homologues.

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